### **SENSORS and TRANSDUCERS**

### Tadeusz Stepinski, Signaler och system

- † The Mechanical Energy Domain
  - Physics
  - Surface acoustic waves
  - Silicon microresonators
  - Variable resistance sensors
  - Piezoelectric sensors
  - Capacitive sensors



## Mechanical Energy Domain

- \* Mechanical transducers are used for determination of quantities such as:
  - Position and (angle) displacement
  - Speed, acceleration
  - Weight and pressure
  - Surface flatness
  - Torsion
  - Vibrations



- \* Basic physical phenomena used for mechanical transducers:
  - Variable resistance
  - Variable inductance
  - Piezoresistivity effect
  - Piezojunction effect
  - Piezoelectric effect
  - Capacitive effect
  - Surface acoustic waves (SAWs)
  - Microresonators



#### Piezoresistivity

In 1954 it was discovered that Ge and Si have 100 times higher piezoresistivity than metals.

Resistivity change of a conductor

$$R'_{S} = \frac{l'r'}{S'} = \frac{l + \Delta l}{S + \Delta S} (r + \Delta r) \quad \text{where:} \quad R' - \text{resistance under pressure}$$

$$\frac{dR}{R} = \frac{dr}{r} + \frac{dl}{l} - \frac{dS}{S}$$

$$P - \text{resistivity}$$

$$S - \text{cross section of the wire}$$

#### † Piezoresistivity

Poisson ratio = (relative change of diameter)/(relative change in length)

$$n = \frac{dD/D}{dl/l} = \frac{e_D}{e_L}$$

Gauge factor for strain gauges

$$K = \frac{(dR/R)}{e_L} = 1 + 2n + \frac{dr/r}{e_L}$$

Can be understood as the ratio of relative change in resistance and the relative change in length. Often the resistivity, r, is considered a constant and the gauge factor

$$K = 1 + 2n$$



### † Piezoresistivity

- -For metals the K factor is about 2
- -For silicon K factor is much higher

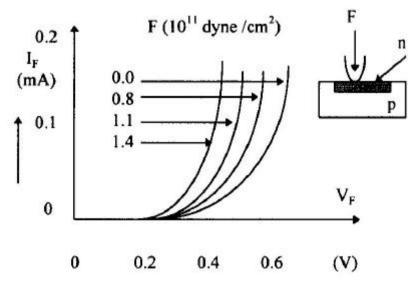
Crystal orientation	n-type Si K factor	p-type Si K factor		
[111]	-13	173		
[110]	-89	121		
[100]	-153	5		

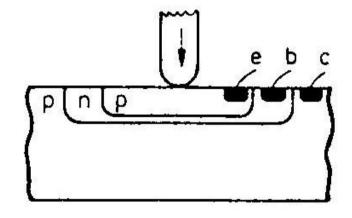
- -Disadvantages of silicon as material for strain gauges:
  - » Brittle material
  - » High temperature coefficient



### † Piezojunction effect

-A change in I-V characteristic when a p-n junction is subjected to mechanical strain







#### † Piezoelectricity

- -A reversible effect not found in Si and Ge
  - » A voltage connected to the material a mechanical change can be observed
  - » A mechanical force applied to the material an electrical tension can be observed
- -When piezoelectricity is present in materials there is no centre of symmetry

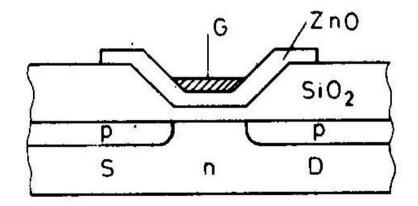
Crystal structure	I	II	III	IV	٧	VI	VII
Centrosymmetric				Si <sup>4+</sup>			
Centrosymmetric				Ge <sup>4+</sup>			
Acentric			Ga <sup>3+</sup>		As <sup>3-</sup>		
Acentric		Cd <sup>2+</sup>				$S^{2-}$	
Acentric		$Zn^{2+}$				$O^{2-}$	
Centrosymmetric	Na⁺						Cl



### † Piezoelectricity

-Example: PI-DMOS

Layers of CdS or ZnO are deposited on silicon substrates to obtain pressure transducers





### † Capacitive effect

-A change of capacitance is measured as a function of stress

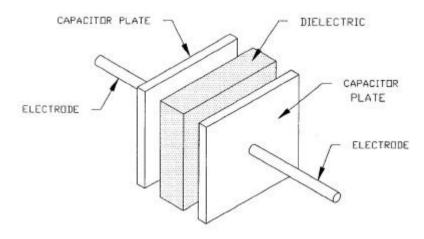
$$C = e_r e_0 \frac{A}{d}$$

 $e_r$  - relative oermittivity

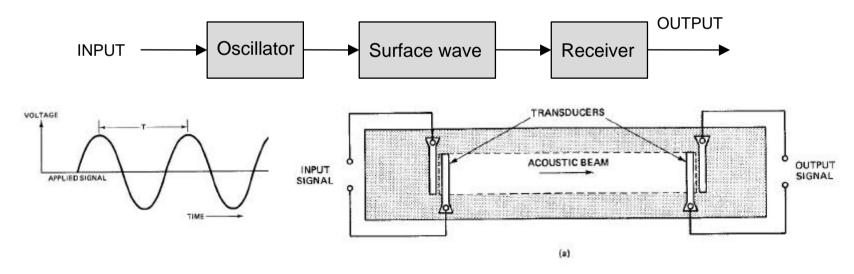
$$e_0 - 8.854 \ 10^{-12} \ F \ m^{-1}$$

d - distance between the plates m

A - area of the plates  $m^2$ 



- Surface acoustic waves (SAW)
  - -Transducers that convert electric signal at the input to an acoustic signal and then again to an electrical signal at the output

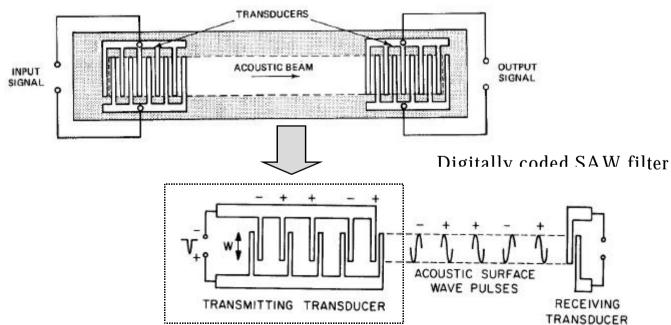




### Surface Acoustic Waves

Surface acoustic waves (SAW)

Multiple electrodes tuned to the same frequency generate Reyleigh wave Substrate lithium niobiate





### Surface Acoustic Waves

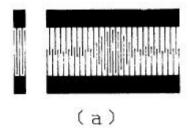
Surface acoustic waves (SAW)

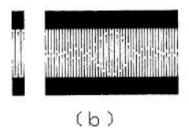
Standard **uniform transducer** has N fingers with constant length and uniform finger pair spacing. Its frequency response takes the form of sinc(x)

$$|H(x)| \approx 2gN \cdot \left| \frac{\sin x}{x} \right| \quad where \quad x = \frac{Np(W - W_0)}{W_0}$$

W<sub>0</sub>- center frequency of the transducer

**Apodized transducer** - by tapering the length of fingers and their spacing, the spectral response of the transducer can be tailored to any given characteristic.





### **Microresonators**

#### \* Silicon microresonators

- Resonant microsensor (microresonator) a device with a mechanical element at resonating frequency which outputs the resonance frequency changes as a function of a physical or chemical parameter.
- Microresonators take the form of cantilevers, micro tuning forks and diaphragms
- Center frequency of cantilever

$$f = 0.16 \cdot \frac{t}{l^2} \cdot \sqrt{\frac{E}{r}}$$

where: l, t (m) - length respective thickness of the tongue

E (Pa) - modulus of elasticity

 $\rho$  (kgm<sup>-3</sup>) - specific mass

# Mechanical Energy Domain - Microresonators

- Microresonator types
  - Vibrating strings
  - Vibrating beams
  - Vibrating capsules
- \* Excitation and detection in silicon microresonators can be performed in different ways:
  - »Electrostatic excitation two electrodes in close proximity
  - »Piezoelectric excitation- built-in piezoelectric material
  - »Resistive heating excitation integrated diffused resistor
  - »Optical heating excitation periodically activated laser
  - »Magnetic excitation electric current + magnetic current



† Potentiometers

Sensing position and angle

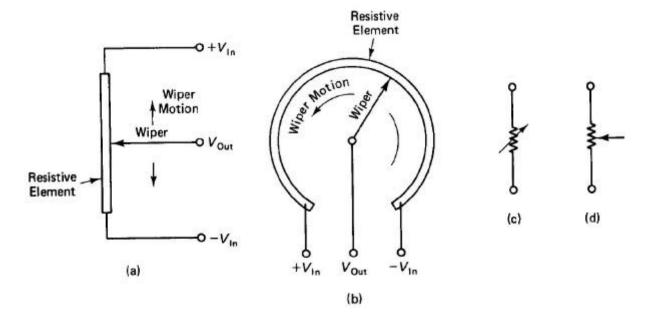
† Strain gauges

Sensing strain and pressure

Voltage divider rule:

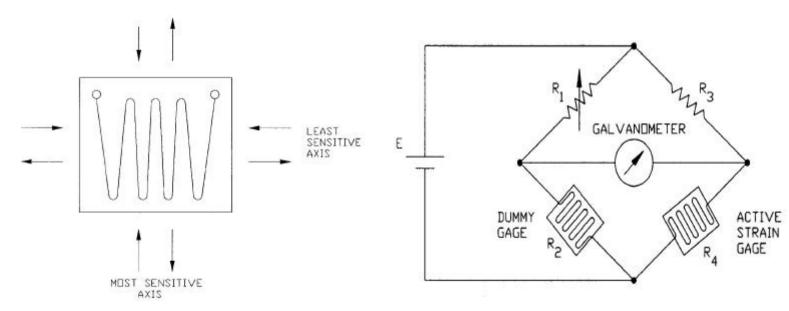
$$E_{out} = r \cdot I_T = r \cdot \frac{E_s}{R + r}$$

#### † Potentiometers





- † Strain gauges
  - Principle

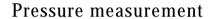


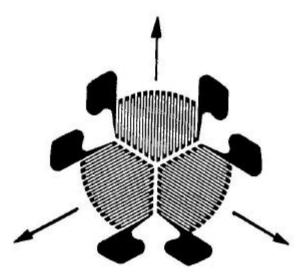


### † Strain gauges

- Practical realization

Strain measurement - 3 axes



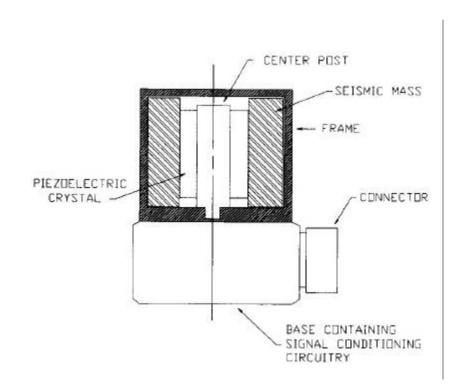






## Piezoelectric sensors

### † Crystal Accelerometers

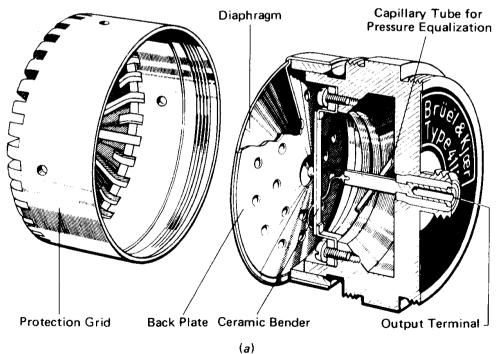




## Piezoelectric sensors

### † Piezoelectric microphone

Ceramic bender is made of piezoelectric material PZT (lead ziroconate titanate)

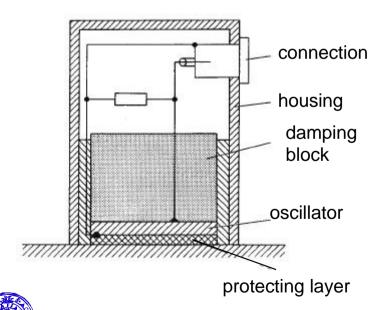




### Piezoelectric sensors

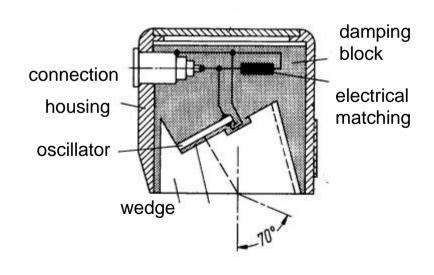
† Piezoelectric ultrasonic transducers for nondestructive evaluation of materials

Normal contact transducer



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Angle transducer



### † Principle

$$C = \frac{\mathbf{e} \cdot A}{d}$$

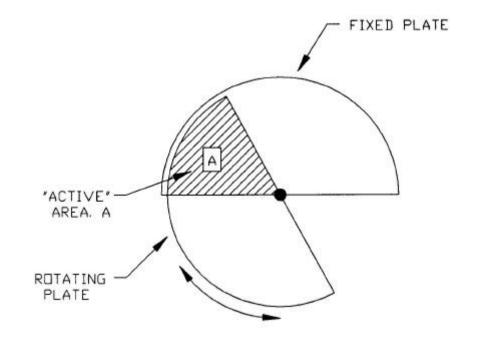
where:

C - capacitance (F)

 $\epsilon$  -permittivity (F/m)

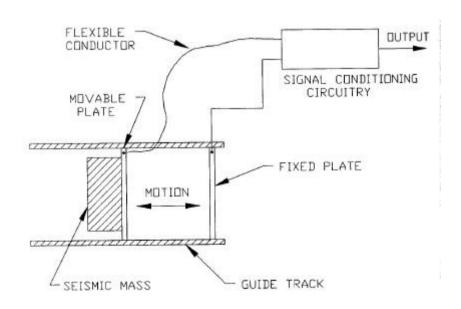
A - area (m<sup>2)</sup>

 $\boldsymbol{S}$  - separation distance of plates (m)



### † Applications

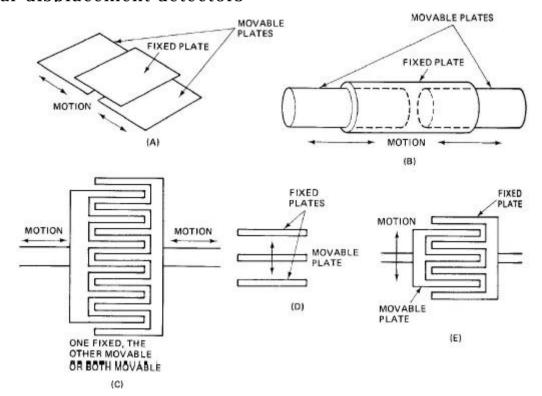
- Seismic mass for detecting acceleration





### † Applications

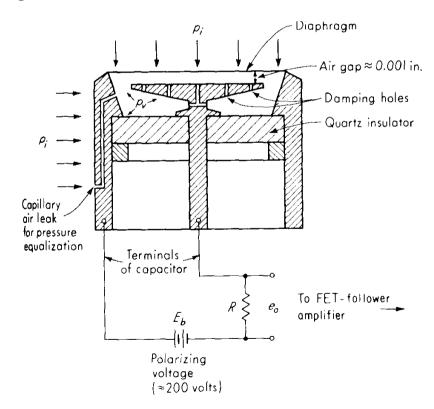
- Linear displacement detectors





### † Applications

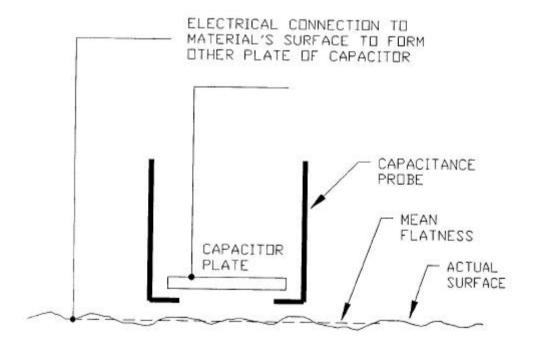
- Capacitor microphone





### † Applications

- Surface roughness detection





## Review Questions

- Describe one application of piezojunction effect
- Explain in detail how SAW filter operates
- What is a strain gage? Explain how it works and give an example of an application
- Explain the function of a dummy gage in a strain gage setup
- Describe at least two types of mechanical construction techniques used in making linear capacitive sensors
- What advantage is there is using multiple-plate capacitive sensors rather than single-plate sensors?
- Explain in detail how a piezoelectric substance is used in conjunction with seismic mass to produce accelerometer
- If quartz and piezoelectric crystal are not electrically conductive, explain how it appears that a current is "conducted through" these substances at their resonant frequencies.

