Digital Communications I: Modulation and Coding Course

> Term 3 - 2008 Catharina Logothetis Lecture 7

#### Last time we talked about:

- Another source of error due to filtering effect of the system:
  - Inter-symbol interference (ISI)
- The techniques to reduce ISI
  - Pulse shaping to achieve zero ISI at the sampling time
  - Equalization to combat the filtering effect of the channel

## Today, we are going to talk about:

- Some bandpass modulation schemes used in DCS for transmitting information over channel
  - M-PAM, M-PSK, M-FSK, M-QAM
- How to detect the transmitted information at the receiver
  - Coherent detection
  - Non-coherent detection

#### Block diagram of a DCS



#### **Bandpass modulation**

- Bandpass modulation: The process of converting a data signal to a sinusoidal waveform where its amplitude, phase or frequency, or a combination of them, are varied in accordance with the transmitting data.
- Bandpass signal:

$$s_i(t) = g_T(t) \sqrt{\frac{2E_i}{T}} \cos\left(\omega_c t + (i-1)\Delta \omega t + \phi_i(t)\right) \quad 0 \le t \le T$$

where  $g_T(t)$  is the baseband pulse shape with energy  $E_{g}$ .

- We assume here (otherwise will be stated):
  - $g_T(t)$  is a rectangular pulse shape with unit energy.
  - Gray coding is used for mapping bits to symbols.
  - $E_s$  denotes average symbol epergy given by  $E_s = \frac{1}{M} \sum_{i=1}^{M} \frac{E_i}{5^i}$

#### **Demodulation and detection**

- Demodulation: The receiver signal is converted to baseband, filtered and sampled.
- Detection: Sampled values are used for detection using a decision rule such as the ML detection rule.



## **Coherent detection**

#### Coherent detection

- requires carrier phase recovery at the receiver and hence, circuits to perform phase estimation.
- Sources of carrier-phase mismatch at the receiver:
  - Propagation delay causes carrier-phase offset in the received signal.
  - The oscillators at the receiver which generate the carrier signal, are not usually phased locked to the transmitted carrier.

#### Coherent detection ..

Circuits such as Phase-Locked-Loop (PLL) are implemented at the receiver for carrier phase estimation ( α ≈ α̂ ).



## **Bandpass Modulation Schemes**

- One dimensional waveforms
  - Amplitude Shift Keying (ASK)
  - M-ary Pulse Amplitude Modulation (M-PAM)
- Two dimensional waveforms
  - M-ary Phase Shift Keying (M-PSK)
  - M-ary Quadrature Amplitude Modulation (M-QAM)
- Multidimensional waveforms
  - M-ary Frequency Shift Keying (M-FSK)

# One dimensional modulation, demodulation and detection

#### Amplitude Shift Keying (ASK) modulation:

$$s_i(t) = \sqrt{\frac{2E_i}{T}} \cos(\omega_c t + \phi)$$

$$s_{i}(t) = a_{i} \psi_{1}(t) \quad i = 1, \dots, M$$
$$\psi_{1}(t) = \sqrt{\frac{2}{T}} \cos(\omega_{c} t + \phi)$$
$$a_{i} = \sqrt{E_{i}}$$

**On-off keying (M=2):** 



#### One dimensional mod.,...

#### M-ary Pulse Amplitude modulation (M-PAM)

$$s_i(t) = a_i \sqrt{\frac{2}{T}} \cos(\omega_c t)$$

$$s_{i}(t) = a_{i} \psi_{1}(t) \quad i = 1, ..., M$$
  

$$\psi_{1}(t) = \sqrt{\frac{2}{T}} \cos(\omega_{c} t)$$
  

$$a_{i} = (2i - 1 - M) \sqrt{E_{g}}$$
  

$$E_{i} = \|\mathbf{s}_{i}\|^{2} = E_{g} (2i - 1 - M)^{2}$$
  

$$E_{s} = \frac{(M^{2} - 1)}{3} E_{g}$$

**4-PAM:** 



#### Example of bandpass modulation: Binary PAM



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## One dimensional mod.,...-cont'd

#### Coherent detection of M-PAM



Two dimensional modulation, demodulation and detection (M-PSK)

M-ary Phase Shift Keying (M-PSK)

$$s_i(t) = \sqrt{\frac{2E_s}{T}} \cos\left(\omega_c t + \frac{2\pi i}{M}\right)$$

$$s_{i}(t) = a_{i1} \psi_{-1}(t) + a_{i2} \psi_{-2}(t) \quad i = 1, \dots, M$$
  
$$\psi_{-1}(t) = \sqrt{\frac{2}{T}} \cos(\omega_{c} t) \quad \psi_{-2}(t) = -\sqrt{\frac{2}{T}} \sin(\omega_{c} t)$$
  
$$a_{i1} = \sqrt{E_{s}} \cos\left(\frac{2\pi i}{M}\right) \qquad a_{i2} = \sqrt{E_{s}} \sin\left(\frac{2\pi i}{M}\right)$$
  
$$E_{s} = E_{i} = \|\mathbf{s}_{i}\|^{2}$$

## Two dimensional mod.,... (MPSK)

BPSK (M=2)



QPSK (M=4)





## Two dimensional mod.,...(MPSK)

#### Coherent detection of MPSK



## Two dimensional mod.,... (M-QAM)

M-ary Quadrature Amplitude Mod. (M-QAM)

$$s_i(t) = \sqrt{\frac{2E_i}{T}} \cos(\omega_c t + \varphi_i)$$

## Two dimensional mod.,... (M-QAM)





## Two dimensional mod.,... (M-QAM)

#### Coherent detection of M-QAM



## Multi-dimensional modulation, demodulation & detection

M-ary Frequency Shift keying (M-FSK)

$$s_{i}(t) = \sqrt{\frac{2E_{s}}{T}} \cos(\omega_{i}t) = \sqrt{\frac{2E_{s}}{T}} \cos(\omega_{c}t + (i-1)\Delta \omega_{c}t)$$

$$\Delta f = \frac{\Delta \omega}{2\pi} = \frac{1}{2T}$$

$$s_{i}(t) = \sum_{j=1}^{M} a_{ij} \psi_{j}(t) \quad i = 1, \dots, M$$

$$\psi_{i}(t) = \sqrt{\frac{2}{T}} \cos(\omega_{i}t) \quad a_{ij} = \begin{cases} \sqrt{E_{s}} & i = j\\ 0 & i \neq j \end{cases}$$

$$E_{s} = E_{i} = \|\mathbf{s}_{i}\|^{2}$$

$$\text{Lecture 7}$$

$$v_{1}(t) = \sqrt{\frac{2}{T}} \cos(\omega_{i}t) = 20$$

#### Multi-dimensional mod.,...(M-FSK)



- Non-coherent detection:
  - No need for a reference in phase with the received carrier
  - Less complexity compared to coherent detection at the price of higher error rate.

- Differential coherent detection
  - Differential encoding of the message
    - The symbol phase changes if the current bit is different from the previous bit.

$$s_{i}(t) = \sqrt{\frac{2E}{T}} \cos\left(\omega_{0}t + \theta_{i}(t)\right), \quad 0 \le t \le T, \quad i = 1, \dots, M$$
$$\theta_{k}(nT) = \theta_{k}((n-1)T) + \phi_{i}(nT)$$

Symbol index: kData bits:  $m_k$ Diff. encoded bits Symbol phase:  $\theta_k$ 



- Coherent detection for diff encoded mod.
  - assumes slow variation in carrier-phase mismatch during two symbol intervals.
  - correlates the received signal with basis functions
  - uses the phase difference between the current received vector and previously estimated symbol  $r(t) = \sqrt{\frac{2E}{T}} \cos\left(\omega_0 t + \theta_i(t) + \alpha\right) + n(t), \quad 0 \le t \le T$  $\left(\theta_{i}(nT)+\alpha\right)-\left(\theta_{i}((n-1)T)+\alpha\right)=\theta_{i}(nT)-\theta_{i}((n-1)T)=\phi_{i}(nT)$  $\Psi_2(t)$  $(a_2, b_2)$  $(a_1, b_1)$ Lecture 7



 Performance degradation about 3 dB by using suboptimal detector

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#### Energy detection

- Non-coherent detection for orthogonal signals (e.g. M-FSK)
  - Carrier-phase offset causes partial correlation between I and Q branches for each candidate signal.
  - The received energy corresponding to each candidate signal is used for detection.

