Digital Communications I: Modulation and Coding Course

Term 3 – 2008 Catharina Logothetis Lecture 2

Last time, we talked about:

- Important features of digital communication systems
- Some basic concepts and definitions such as as signal classification, spectral density, random process, linear systems and signal bandwidth.

Today, we are going to talk about:

- The first important step in any DCS:
 - Transforming the information source to a form compatible with a digital system

Formatting and transmission of baseband signal



Format analog signals

- To transform an analog waveform into a form that is compatible with a digital communication system, the following steps are taken:
 - 1. Sampling
 - 2. Quantization and encoding
 - 3. Baseband transmission







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Aliasing effect



Sampling theorem

Analog Sampling Pulse amplitude signal Pulse amplitude modulated (PAM) signal Sampling theorem: A bandlimited signal with no spectral components beyond f_m , can be uniquely determined by values sampled at uniform intervals of

$$T_s \leq \frac{1}{2f_m}$$

The sampling rate, $f_s = \frac{1}{T_s} = 2f_m$ is called Nyquist rate.

Quantization

Amplitude quantizing: Mapping samples of a continuous amplitude waveform to a finite set of amplitudes.





- A uniform linear quantizer is called <u>Pulse Code</u> <u>Modulation</u> (PCM).
- Pulse code modulation (PCM): Encoding the quantized signals into a digital word (PCM word or codeword).
 - Each quantized sample is digitally encoded into an *l* bits codeword where *L* in the number of quantization levels and

$$l = \log_2 L$$



Quantization error

Quantizing error: The difference between the input and output of a quantizer $\implies e(t) = \hat{x}(t) - x(t)$



Quantization error ...

Quantizing error:

- Granular or linear errors happen for inputs within the dynamic range of quantizer
- Saturation errors happen for inputs outside the dynamic range of quantizer
 - Saturation errors are larger than linear errors
 - Saturation errors can be avoided by proper tuning of AGC
- Quantization noise variance:

$$\sigma_{q}^{2} = \mathbf{E}\{[x - q(x)]^{2}\} = \int_{-\infty}^{\infty} e^{2}(x)p(x)dx = \sigma_{\text{Lin}}^{2} + \sigma_{\text{Sat}}^{2}$$
$$\sigma_{\text{Lin}}^{2} = 2\sum_{l=0}^{L/2-1} \frac{q_{l}^{2}}{12}p(x_{l})q_{l} \text{ Uniform q.} \quad \sigma_{\text{Lin}}^{2} = \frac{q^{2}}{12}$$

Uniform and non-uniform quant.

- Uniform (linear) quantizing:
 - No assumption about amplitude statistics and correlation properties of the input.
 - Not using the user-related specifications
 - Robust to small changes in input statistic by not finely tuned to a specific set of input parameters
 - Simple implementation
 - Application of linear quantizer:
 - Signal processing, graphic and display applications, process control applications
- Non-uniform quantizing:
 - Using the input statistics to tune quantizer parameters
 - Larger SNR than uniform quantizing with same number of levels
 - Non-uniform intervals in the dynamic range with same quantization noise variance
 - Application of non-uniform quantizer:
 - Commonly used for speech

Non-uniform quantization

- It is achieved by uniformly quantizing the "compressed" signal.
- At the receiver, an inverse compression characteristic, called "expansion" is employed to avoid signal distortion.



Statistics of speech amplitudes

In speech, weak signals are more frequent than strong ones.



- Using equal step sizes (uniform quantizer) gives low $\left(\frac{S}{N}\right)_q$ for weak signals and high $\left(\frac{S}{N}\right)_q$ for strong signals.
 - Adjusting the step size of the quantizer by taking into account the speech statistics improves the SNR for the input range.

Baseband transmission

- To transmit information through physical channels, PCM sequences (codewords) are transformed to pulses (waveforms).
 - Each waveform carries a symbol from a set of size M.
 - Each transmit symbol represents $k = \log_2 M$ bits of the PCM words.
 - PCM waveforms (line codes) are used for binary symbols (M=2).
 - M-ary pulse modulation are used for non-binary symbols (M>2).

PCM waveforms

PCM waveforms category:

Nonreturn-to-zero (NRZ)

Return-to-zero (RZ)

- Phase encoded
 - Multilevel binary



PCM waveforms ...

- Criteria for comparing and selecting PCM waveforms:
 - Spectral characteristics (power spectral density and bandwidth efficiency)
 - Bit synchronization capability
 - Error detection capability
 - Interference and noise immunity
 - Implementation cost and complexity

Spectra of PCM waveforms



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M-ary pulse modulation

M-ary pulse modulations category:

- M-ary pulse-amplitude modulation (PAM)
- M-ary pulse-position modulation (PPM)
- M-ary pulse-duration modulation (PDM)
- M-ary PAM is a multi-level signaling where each symbol takes one of the *M* allowable amplitude levels, each representing $k = \log_2 M$ bits of PCM words.
- For a given data rate, M-ary PAM (M>2) requires less bandwidth than binary PCM.
- For a given average pulse power, binary PCM is easier to detect than M-ary PAM (M>2).

PAM example



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